

# Complementary Limb Motion Estimation for the Control of Active Knee Prostheses

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**Abstract**—To restore walking after transfemoral amputation, various actuated exoprostheses have been developed, which control the knee torque actively or via variable damping. In both cases, an important issue is to find the appropriate control that enables user-dominated gait. Recently, we suggested a generic method to deduce intended motion of impaired or amputated limbs from residual human body motion. Based on interjoint coordination in physiological gait, statistical regression is used to estimate missing motion. In a pilot study, this Complementary Limb Motion Estimation (CLME) strategy is applied to control an active knee exoprosthesis. A motor-driven prosthetic knee with one Degree of Freedom has been realized, and one above-knee amputee has used it with CLME. Performed tasks are walking on a treadmill and alternating stair ascent and descent. The subject was able to walk on the treadmill at varying speeds, but needed assistance with the stairs, especially to descend. The promising results with CLME are compared to the subject's performance with her own prosthesis, the C-Leg from Otto Bock.

## Keywords

Active Prostheses, Intention Estimation, User-Cooperative Control

## I. INTRODUCTION

Physiological human gait is a continuous control process, which allows adaptation to almost arbitrary environments on the basis of a broad experience. Human capabilities in the coordination of movements still outperform biped robots by far. After the loss of a leg due to amputation, the motor system is generally still capable of these complex control tasks, and the ideal of a prosthetic solution would be a seamless integration into the sensorimotor control loop. On this way, there are two challenges: One is to realize a portable hardware solution that is capable of generating the same forces

and movements as a human leg. The second challenge is to interface the prosthesis with the human controller.

The first hardware solutions were passive mechanical joints. Using monocentric and later polycentric knee joints, stable stance and also knee flexion during swing were possible. A major advance was marked by the development of adaptively damped devices, namely the C-Leg (Otto Bock HealthCare GmbH, Duderstadt, Germany) and the Rheo Knee (Össur Inc., Reykjavík, Iceland). These systems exploit the fact that knee joint power during physiological gait is mainly negative, meaning that the muscles are predominantly active to decelerate and to absorb energy. With very little power supply, microprocessor-controlled fluidic dampers can adapt the viscous torque according to the current gait phase, enabling a near-normal gait pattern. Microprocessor-controlled joints show biomechanical advantages compared to passive mechanical joints, like smoother gait and less compensatory hip activity on the contralateral side [18]. Furthermore, they show an improved behavior when descending stairs and negotiating rough terrain, and they can reduce the risk of stumbling and falls [17].

However, knee joint power is low during gait, but it is not zero. Thus, purely dissipative devices are still a compromise and cannot enable fully physiological gait. Furthermore, they do not allow movements that intrinsically depend on positive knee power, like alternating stair ascent. Powered prostheses are becoming more popular, but they pose considerable engineering challenges, mainly due to power and energy requirements. Early experimental platforms are therefore tethered, like the hydraulic knee prosthesis presented in [8], or they have a limited range, like the battery-powered prosthesis with electrical motors presented in [23]. Recent developments in actuator and energy storage technology can alleviate the problem of weight and range (see e.g. [11]). The only commercial device is the Power Knee from Össur and Victrom Human Bionics, Canada. However, there are various systems in a research stage, like a pneumatic prosthesis [26], a prosthetic knee with Series Elastic Actuation [21], and a hybrid concept that combines dissipative and active elements using hydraulics and an electric pump [20].

Given controlled dissipative or active platforms, many options open up for control design. However, the integration into the human control apparatus is challenging.

Current exoprosthetic controllers exhibit a high degree of intelligence: They work with sophisticated rules [24], gait-phase dependent damping like the C-Leg (Otto Bock) or

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the Rheo Knee (Össur), with variable stiffness [26], or with artificial reflexes [6]. What is problematic in these intelligent devices is the accompanying autonomy: The user does not have direct control over the leg. Clinical studies show that patients can feel forced to adapt to the system [28].

There have been attempts to integrate prosthesis control more tightly with human sensorimotor control. One applicable strategy could be the use of electromyography (EMG), which measures motor commands sent to the muscles. This method has been applied to hand prostheses [4] and exoskeletons [7], [19], and it has been attempted also for knee prostheses [5]. For the upper extremities, the surgical procedure of Targeted Muscle Reinnervation already allows dexterous control of multiple degrees of freedom [22]. However, a disadvantage of EMG is its high sensitivity to noise, especially when non-invasive methods are used. For a leg prosthesis, robustness is crucial. Furthermore, EMG cannot be used for all patients.

A key to estimating user intention may be to observe residual body motion. An early approach was made by simply “echoing” the motion of the residual leg to the other side [12]. However, a major disadvantage is the time delay of one step that is introduced between human and prosthetic actions. A similar approach is taken by the control of the the Power Knee: Its “Sound-Side Sensory Control” allows various movement primitives, with their number and type limited by an explicit state machine [2]. The prosthetic leg is synchronized with motion of the contralateral sound leg, which is possible due to sensors in a shoe insole. However, such an approach limits the use to cyclic, symmetric patterns, and it requires initiating new motions with the sound side. Furthermore, it cannot be used for bilateral amputees.

Recently, we suggested an instantaneous, delay-free approach to motion intention estimation of missing or paralyzed limbs [13], [16]. This approach, Complementary Limb Motion Estimation (CLME), observes residual body motion, and it continuously complements this motion for missing limbs by simple regression. This is possible because physiological human motion exhibits strong interjoint coordination [25], enabling statistical estimation of missing movements. CLME should not be confounded with the above mentioned echo-control approaches, which replay the recorded motion of one leg with a time shift on the other side. In contrast, CLME offers a continuous and instantaneous complementation of motion. Initially developed for robot-aided gait rehabilitation of hemiparetic patients, CLME has been successfully tested on a rehabilitation robot [15], [16].

In this paper, we show how CLME can be transferred to active prostheses. To allow a first practical evaluation, a simple actuated prosthesis has been realized. The device is used in combination with sensors to measure angles and velocities of the user’s residual body motion. We show data of an amputee subject walking on a treadmill, as well as ascending and descending stairs.

## II. MATERIALS AND METHODS

### A. Complementary Limb Motion Estimation (CLME)

The goal of Complementary Limb Motion Estimation is to find a mapping function that outputs the states of missing limbs (angles and velocities) in dependence of the states of residual human limbs. To obtain this function, interjoint coordination patterns are extracted from recorded physiological movement trajectories. Then, a reference motion is generated on-line for exoprosthetic joints, using the current motion of the residual limbs.

To find a static mapping that gives prosthetic joint motion as a function of residual human joint motion, there are numerous approaches in statistical regression. A simple linear mapping has shown acceptable results in past experiments in robot-aided gait rehabilitation [16], so a function of the type

$$\begin{pmatrix} \varphi_p \\ \dot{\varphi}_p \end{pmatrix} = \mathbf{K} \begin{pmatrix} \varphi_h \\ \dot{\varphi}_h \end{pmatrix} + \mathbf{k} \quad (1)$$

is used, with mapping matrix  $\mathbf{K}$  and offset vector  $\mathbf{k}$ . Here, the motion of the considered human body joints is described by the angle vector  $\varphi_h$  and the vector of angular velocities  $\dot{\varphi}_h$ , and the motion of the prosthetic joints is described by the vectors  $\varphi_p$  and  $\dot{\varphi}_p$  for angles and velocities, respectively.

To obtain  $\mathbf{K}$  and  $\mathbf{k}$ , conventional Best Linear Unbiased Estimation (BLUE) is used here as the baseline approach to regression [1]. First, a given movement pattern (e.g. level gait) is recorded from a non-impaired subject, and mean values ( $\bar{\varphi}$  and  $\bar{\dot{\varphi}}$ ) and standard deviations (subsumed in the diagonal matrix  $\mathbf{S}$ ) are extracted for all joints. Using this information, the normalized state vector  $\mathbf{x}_h$  is defined, containing only the data of human joints that will also be available in the amputee subject:

$$\mathbf{x}_h := \mathbf{S}_h^{-1} \left[ \begin{pmatrix} \varphi_h \\ \dot{\varphi}_h \end{pmatrix} - \begin{pmatrix} \bar{\varphi}_h \\ \bar{\dot{\varphi}}_h \end{pmatrix} \right]. \quad (2)$$

The same is done for the states of the prosthetic joint(s):

$$\mathbf{x}_p := \mathbf{S}_p^{-1} \left[ \begin{pmatrix} \varphi_p \\ \dot{\varphi}_p \end{pmatrix} - \begin{pmatrix} \bar{\varphi}_p \\ \bar{\dot{\varphi}}_p \end{pmatrix} \right]. \quad (3)$$

The estimate of  $\mathbf{x}_p$  as a function of  $\mathbf{x}_h$  is then found by minimizing the expected error

$$E(\|\mathbf{x}_p - \mathbf{C}\mathbf{x}_h\|^2) \rightarrow \min \quad (4)$$

in terms of the constant matrix  $\mathbf{C}$ . Using the covariance matrices  $\mathbf{M}_{hh}$  and  $\mathbf{M}_{hp}$  of the respective data vectors in recorded physiological motion, the solution is given by:

$$\mathbf{C} = (\mathbf{M}_{hh}^{-1}\mathbf{M}_{hp})^T, \quad \hat{\mathbf{x}}_p = \mathbf{C}\mathbf{x}_h. \quad (5)$$

The outputs are augmented with mean and standard deviation of the physiological motion, which gives reference angle and velocity for the prosthetic joint(s). In summary, the coefficients in  $\mathbf{K}$  and  $\mathbf{k}$  in (1) are obtained by:

$$\mathbf{K} = \mathbf{S}_p\mathbf{C}\mathbf{S}_h^{-1}, \quad \mathbf{k} = -\mathbf{K} \begin{pmatrix} \bar{\varphi}_h \\ \bar{\dot{\varphi}}_h \end{pmatrix} + \begin{pmatrix} \bar{\varphi}_p \\ \bar{\dot{\varphi}}_p \end{pmatrix} \quad (6)$$

The estimates are subject to uncertainty, and there could be a discrepancy between estimated velocity and the derivative of the estimated angle. To merge the two pieces of information for each joint, a Kalman filter is used. This filter is designed based on the model of a double integrator, and noise covariance matrices are obtained from the regression error of angle and angular velocity [13], [14].

In this application of an actuated knee prosthesis for the right knee, the observed human joints are chosen as left hip angle  $\varphi_{hip,l}$  and left knee angle  $\varphi_{kn,l}$ . They are used to estimate knee angle  $\varphi_{kn,r}$  for the prosthesis on the right:

$$\varphi_h := (\varphi_{hip,l} \quad \varphi_{kn,l})^T, \quad \varphi_p := (\varphi_{kn,r})^T, \quad (7)$$

with corresponding joint angular velocities. The Kalman filter output provides the reference for a position controller for the joint.

This application shows that the state vectors of observed and prosthetic limbs do not have to be of equal size. There could be other limbs involved as part of  $x_h$ . This would require different or additional sensors, for example to measure trunk inclination. The ipsilateral hip had been included as an additional predictor in preliminary experiments, but this led to unstable oscillating behavior during stance. This effect may be due to the mechanical coupling between hip and knee.

It is possible to include not only the states, i.e. angles and velocities, but also accelerations of residual human joints as inputs to the regression. Regardless of the input, it is also possible to estimate accelerations for the prosthetic joints, to obtain an additional piece of information for the Kalman Filter. Simulations indicated that if angles and velocities are available, additional measurement of accelerations hardly improves estimation performance [14].

In summary, a recorded reference motion is reduced to the coefficients in  $\mathbf{K}$  and  $\mathbf{k}$  and the Kalman gains. Based on these parameters and driven by sound limb motion, on-line estimation provides a position reference for the prosthetic joint(s). Thus, CLME automatically exploits the observed kinematic correlations between joints, no explicit knowledge of the motion (e.g. the gait phase) is needed.

## B. Experimental Setup and Data Acquisition

The experimental setup consists of an actuated knee joint, as well as angle and angular velocity sensors attached to the contralateral hip and knee (Fig. 1).

The knee joint is actuated by a Maxon RE 40 DC motor with a planetary gear with transmission ratio  $i = 91$ . To measure knee angle, the motor is equipped with an optical quadrature encoder. The knee joint can be attached easily to the patient's individual prosthetic shaft and foot using standard pyramid adapters. Flexion/extension angles and velocities of hip and knee joint are measured using goniometer-gyroscope units, as described in [9], [10]. Their redundant design with two potentiometers per unit, connected by a telescopic shaft, allows to measure angles without requiring any joint alignment. They are attached to the body using velcro straps.

As the focus of this project is not on hardware development, but on control, the device is tethered and depends on an external power supply. Control and data acquisition is realized via MATLAB/Simulink and RTAI Linux running on a desktop PC at a rate of 1 kHz. This PC, electronics, and the power supply are mounted on a cart that can be moved with the human subject. Safety mechanisms include mechanical and software end stops, as well as manual emergency stop switches.

To obtain the mapping matrices for the CLME controller, a non-impaired 23-year-old female subject walked on a treadmill at a speed of 3 km/h, as well as up and down stairs, equipped with the goniometer-gyroscope units to measure knee and hip flexion angles and velocities on both legs. Then, the interjoint coupling matrix  $\mathbf{C}$ , as well as statistical information for normalization were extracted from the recorded data, as described above. The mapping coefficients are given in the appendix.

A 42-year old female subject with transfemoral amputation took part in this case study and walked on a treadmill, as well as up and down stairs with the previously extracted couplings of the non-impaired subject. The subject was allowed to hold on to the bars during treadmill walking and to the handrail of the stairs, respectively. Furthermore, an assisting person secured her on the stairs.

Reflective markers were attached to the hip, knee, heel, forefoot, and ankle, in order to allow later motion analysis ((Fig. 1). One camera was used to subsequently record the marker positions of left and right side during treadmill walking. To compensate for changes in perspective in these two-dimensional recordings (e.g. due to not perfectly symmetric camera positions on left and right side), a linear transformation of the recorded data points was performed, using known side-symmetric landmarks on the treadmill and Least-Squares optimization. Stair trials were also captured, but only for video documentation, as markers were not visible.

Treadmill walking was compared between CLME-controlled walking and gait with the C-Leg, especially concerning the level of symmetry and the presence of compensatory motion. Symmetry was assessed by comparing the stance-to-swing ratio between legs, which denotes the time ratio spent for each leg with and without ground contact. "Toe

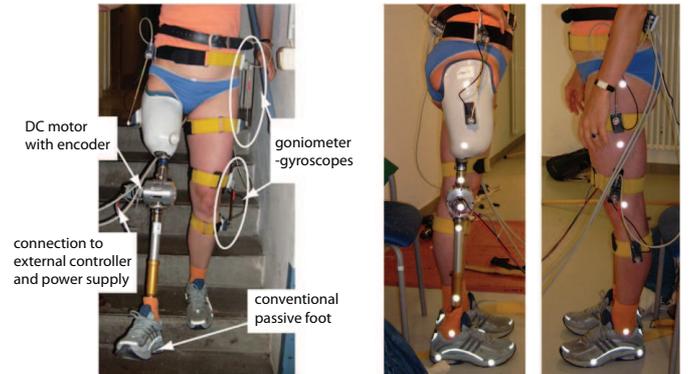


Fig. 1. Experimental Setup (left) and marker placement for gait analysis (right).

off” and “Heel Strike” events were detected by off-line analysis of the kinematic data. Stair descent was compared only qualitatively to the same motion with the C-Leg; alternating stair ascent is not possible with the C-Leg.

### III. RESULTS

The theoretically expected reconstruction accuracy can be illustrated using off-line analysis of the non-impaired subject’s recorded gait pattern. Fig. 2 shows the result when the mapping is applied to estimate knee motion of one side from knee and hip motion of the contralateral side. The linear regression reconstructs knee angular velocity better than angle. However, it can be seen that the Kalman filter uses both pieces of information and improves angle estimation quality.

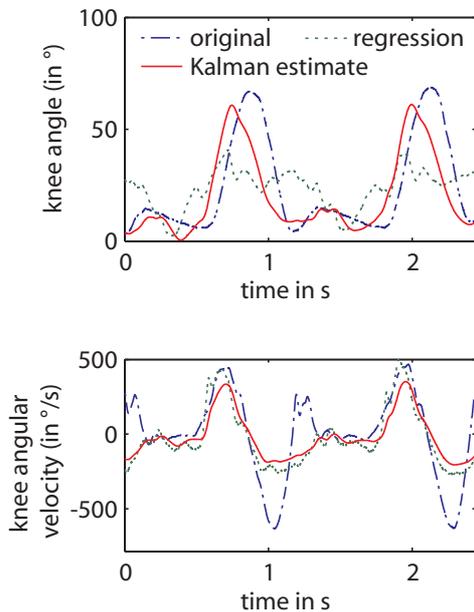


Fig. 2. Theoretical estimation accuracy when applying the regression and filtering to the off-line stored gait data of the non-impaired reference subject.

With this mapping, the amputee subject was able to walk smoothly after a few minutes of practice. She noticed how left and right leg were coupled, and she also managed to alter her gait voluntarily. She was able to walk at varying velocities (tested up to 5 km/h) with the same controller.

Compared to walking with the C-Leg, the subject made longer steps with her sound leg, such that asymmetry slightly increased. This is reflected in the average stance-to-swing ratio: For the C-Leg, this ratio was 1.09 and 1.38 for right and left leg at 4 km/h, respectively. For the CLME-controlled prosthesis, the corresponding values were 0.99 and 1.40. The difference between C-Leg and CLME control is significant only for the right, prosthetic leg ( $p=0.00091$ ), but not for the left leg ( $p=0.18$ ).

A qualitative observation was that the subject vaulted slightly on her sound leg when walking with the C-Leg. This did not occur with the CLME-controlled prosthesis. In the trajectories of the heel marker during walking with the two

devices (Fig. 3), the vaulting can be seen, as well as the increased step size with CLME.

The shape of the knee joint angle trajectories of the sound and of the prosthetic knee joint is shown in Fig. 4, beginning with heel strike. The prosthetic knee does not flex during stance phase, neither for the C-Leg, nor for the CLME-controlled joint.

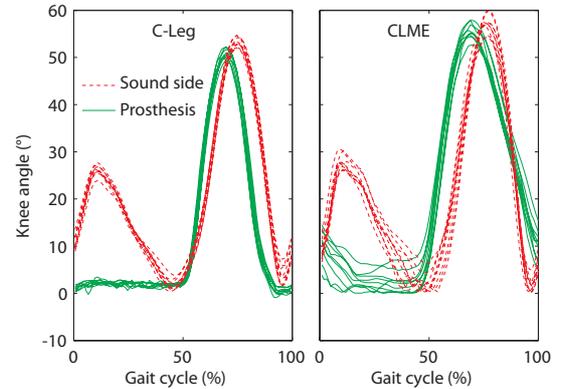


Fig. 4. Knee angle trajectories during treadmill walking with the C-Leg (left) and with a CLME-controlled active knee joint (right). Sound and prosthetic knee joint angles (dashed and solid lines, respectively) are normalized and plotted over multiple steps

Like treadmill walking, the subject also quickly learned how to ascend the stairs smoothly (Fig. 5), starting on either leg. However, she needed assistance with balance, and correct placement of the prosthetic foot on the next step required some compensatory motion with the hip.



Fig. 5. Stair ascent with a CLME-controlled prosthetic knee joint. An assisting person (right) helps with balance. Time between adjacent frames: 40 ms.

In stair descent (Fig. 6), the performance of the CLME-controlled prosthesis was less satisfactory, as it did not match the subject’s smooth stair descent with her C-Leg. The subject reported that she felt insecure, and she hesitated to initiate the next descent with the prosthesis, prolonging the time spent on the sound leg.

### IV. DISCUSSION

The results show that it is generally feasible to control an actuated exoprosthesis by Complementary Limb Motion Estimation. Using a simple mapping function from residual body

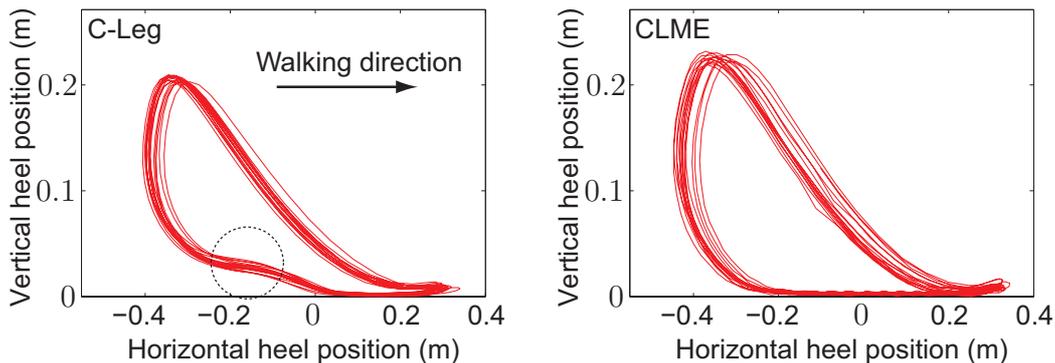


Fig. 3. Cartesian trajectory of the sound leg’s heel during treadmill walking with the C-Leg (left) and with a CLME-controlled active knee joint (right). Vaulting can be observed with the C-Leg.



Fig. 6. Stair descent with a CLME-controlled prosthetic knee joint. An assisting person (left) helps with balance. Time between adjacent frames: 40 ms.

motion to the prosthesis, the volunteer amputee subject was able to achieve an almost physiological gait pattern.

In contrast to walking with the C-Leg, no contralateral vaulting occurred, which can be explained by the fact that the active prosthesis can generate positive power to flex the knee during swing. This eliminates the need for contralateral compensation to clear the foot. CLME also exploits another advantage of a system that can generate positive power, which is to enable alternating stair ascent.

Prolonged stance phases on the sound leg can to some extent be explained by a lack of training of the subject. For example, physiological stair descent is an almost ballistic motion consisting of successive phases of controlled falling. This requires a high level of confidence in the knee joint, which can probably not be achieved in the first minutes with a new device.

The observation that the subject was able to walk at different speeds without change of the mapping function indicates that the mapping is robust for a large range of speeds in level walking.

A major limitation for further evaluation is the current hardware. In addition to being tethered, the prosthetic knee is not a realistic platform, much better realizations are available (like the PowerKnee by Össur or the platforms described in [20], [21], [26]). For example, the motor protrudes from the joint, which leads to inertial torques about the vertical axis.

Also in flexion/extension direction, motor and transmission weight and inertia may have introduced a disturbance.

Alternative or in addition to improving this hardware, it could be interesting to investigate a similar control scheme for controlled dissipative devices, which offer considerable advantages in terms of weight and range.

## V. CONCLUSION AND OUTLOOK

This first proof of concept shows that the minimization of “autonomous intelligence” in an actuated prosthesis combined with close observation of the user allow to incorporate the human’s superior motion control in a cooperative and intuitive way.

Future research will focus on generalizing CLME and adapting it to practical requirements of exoprostheses. The current position control scheme will be replaced by a more compliant control approach. Other extensions will aim to enable seamless transitioning between different activities. This should be done without explicit switching, but by finding a more general mapping. A possible solution for this may be to observe more body parts, or to extend the mapping to the nonlinear domain, possibly using techniques such as Generalized Principal Component Analysis [27] or Correlation Clustering [3]. Finally, the hardware platform needs to be improved in terms of weight and inertia, in order to allow more realistic testing.

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## APPENDIX

The mapping matrix  $\mathbf{K}$  and offset vector  $\mathbf{k}$  in (1) for level gait are:

$$\mathbf{K} = \begin{pmatrix} -0.050 & 0.105 & -0.125 \text{ s} & 0.012 \text{ s} \\ 18.481/\text{s} & 7.911/\text{s} & -1.78 & 0.67 \end{pmatrix},$$

$$\mathbf{k} = \begin{pmatrix} 21.73^\circ \\ -573.82^\circ/\text{s} \end{pmatrix}.$$

The values for stair ascent are:

$$\mathbf{K} = \begin{pmatrix} -1.242 & -0.189 & -0.048 \text{ s} & -0.046 \text{ s} \\ -1.05/\text{s} & 0.79/\text{s} & -0.73 & -0.25 \end{pmatrix},$$

$$\mathbf{k} = \begin{pmatrix} 93.10^\circ \\ 17.08^\circ/\text{s} \end{pmatrix},$$

and for stair descent:

$$\mathbf{K} = \begin{pmatrix} -1.372 & -0.024 & -0.147 \text{ s} & -0.022 \text{ s} \\ 29.49/\text{s} & -1.08/\text{s} & -1.32 & 0.97 \end{pmatrix},$$

$$\mathbf{k} = \begin{pmatrix} 72.82^\circ \\ -705.69^\circ/\text{s} \end{pmatrix}.$$